

## Problem 18

In each of Problems 17 through 20, draw a direction field and plot (or sketch) several solutions of the given differential equation. Describe how solutions appear to behave as  $t$  increases and how their behavior depends on the initial value  $y_0$  when  $t = 0$ .

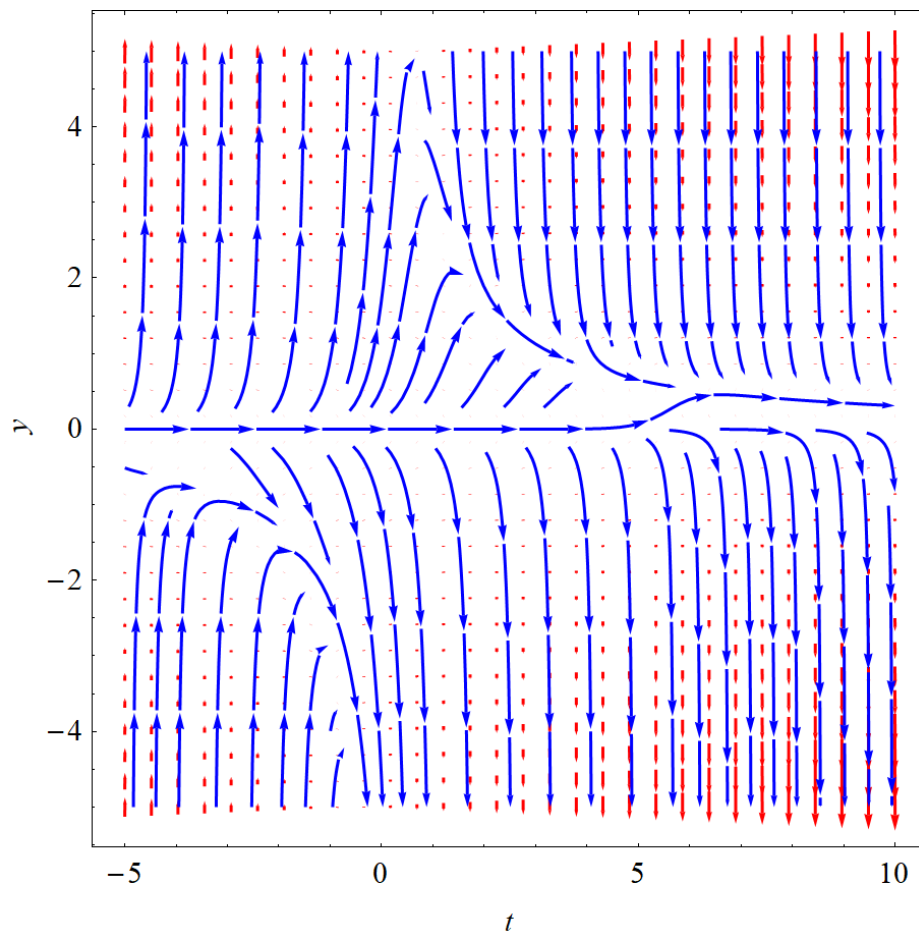
$$y' = y(3 - ty)$$

### Solution

The direction field is the vector field

$$\langle dt, dy \rangle = \left\langle 1, \frac{dy}{dt} \right\rangle dt = \langle 1, y(3 - ty) \rangle dt.$$

Below in red are the field vectors, and in blue are possible solution curves to the ODE, depending on the initial condition  $(t_0, y_0)$ . The solution curves lie tangent to the field vectors at every point and never intersect.



Assuming an initial condition of the form  $y(0) = y_0$ , the solution will tend to  $y = 0$  if  $y_0 \geq 0$  and tend to  $y = -\infty$  if  $y_0 < 0$ .