Problem 4

In each of Problems 1 through 6, use Euler's formula to write the given expression in the form a + ib.

$$e^{2-(\pi/2)i}$$

Solution

Euler's formula states that $e^{ix} = \cos x + i \sin x$. Split up the exponential function first and then use the formula.

$$e^{2-(\pi/2)i} = e^2 \exp\left(-i\frac{\pi}{2}\right)$$

$$= e^2 \left[\cos\left(-\frac{\pi}{2}\right) + i\sin\left(-\frac{\pi}{2}\right)\right]$$

$$= e^2 \left[\cos\left(\frac{\pi}{2}\right) - i\sin\left(\frac{\pi}{2}\right)\right]$$

$$= e^2[0 - i(1)]$$

$$= -e^2i$$

$$\approx -7.39i$$