

Problem 25

In each of Problems 25 through 28, determine whether the given integral converges or diverges.

$$\int_0^\infty (t^2 + 1)^{-1} dt$$

Solution

$$\begin{aligned}\int_0^\infty (t^2 + 1)^{-1} dt &= \tan^{-1} t \Big|_0^\infty \\&= \tan^{-1} \infty - \tan^{-1} 0 \\&= \frac{\pi}{2} - 0 \\&= \frac{\pi}{2}\end{aligned}$$

The integral converges.