

Exercise 32

Solve the inhomogeneous partial differential equation

$$\begin{aligned}u_{xt} &= -\omega \sin \omega t, \quad t > 0, \\u(x, 0) &= x, \quad u(0, t) = 0.\end{aligned}$$