

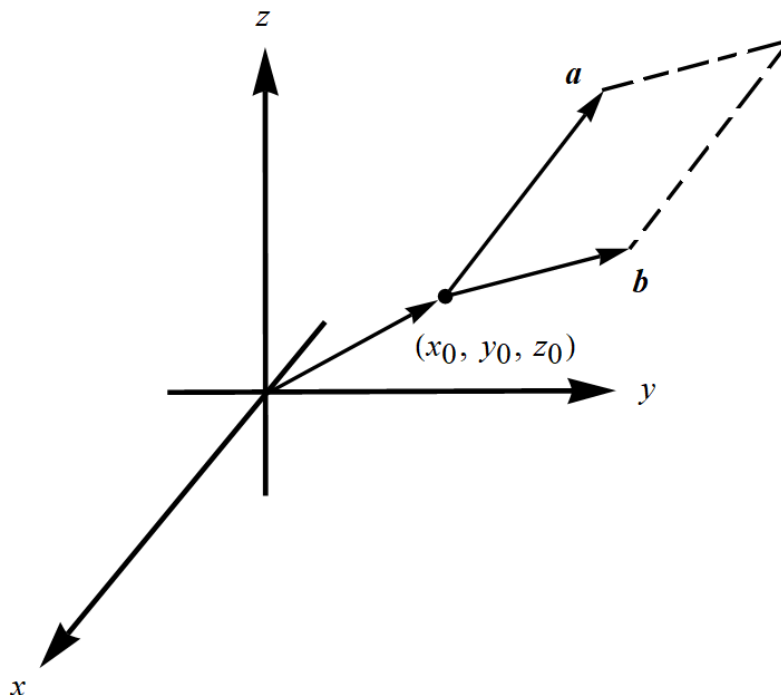
## Exercise 30

In Exercises 29 to 31, use vector methods to describe the given configurations.

The points within the parallelogram with one corner at  $(x_0, y_0, z_0)$  whose sides extending from that corner are equal in magnitude and direction to vectors  $\mathbf{a}$  and  $\mathbf{b}$

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### Solution



Assuming that  $\mathbf{a}$  and  $\mathbf{b}$  are linearly independent, a linear combination of these two spans an entire plane in three-dimensional space.

$$\mathbf{r}(s, t) = s\mathbf{a} + t\mathbf{b}$$

By restricting  $s$  and  $t$  to be between 0 and 1, only the points within the parallelogram with edge vectors,  $\mathbf{a}$  and  $\mathbf{b}$ , are obtained. One of this parallelogram's corners is at the origin ( $s = 0$  and  $t = 0$ ). Adding the position vector  $(x_0, y_0, z_0)$  to  $\mathbf{r}(s, t)$  makes it so that this corner is at  $(x_0, y_0, z_0)$  instead.

$$\{(x_0, y_0, z_0) + s\mathbf{a} + t\mathbf{b}, 0 \leq s \leq 1, 0 \leq t \leq 1\}$$