

**Problem 1**

Find all functions  $f$  such that  $f'$  is continuous and

$$[f(x)]^2 = 100 + \int_0^x \{[f(t)]^2 + [f'(t)]^2\} dt \quad \text{for all real } x$$