

**Exercise 1**

By trial and error, find a solution of the diffusion equation  $u_t = u_{xx}$  with the initial condition  $u(x, 0) = x^2$ .