

Exercise 5

Consider the equation

$$u_x + yu_y = 0$$

with the boundary condition $u(x, 0) = \phi(x)$.

- (a) For $\phi(x) \equiv x$, show that no solution exists.
- (b) For $\phi(x) \equiv 1$, show that there are many solutions.