

Exercise 3

In the cube $(0, a)^3$, a substance is diffusing whose molecules multiply at a rate proportional to the concentration. It therefore satisfies the PDE $u_t = k\Delta u + \gamma u$, where γ is a constant. Assume that $u = 0$ on all six sides. What is the condition on γ so that the concentration does not grow without bound?