

Exercise 3

Show that the wave equation has the following invariance properties.

- (a) Any translate $u(x - y, t)$, where y is fixed, is also a solution.
- (b) Any derivative, say u_x , of a solution is also a solution.
- (c) The dilated function $u(ax, at)$ is also a solution, for any constant a .