

**Exercise 16**

Find the positive eigenvalues and the corresponding eigenfunctions of the fourth-order operator  $+d^4/dx^4$  with the four boundary conditions

$$X(0) = X(l) = X''(0) = X''(l) = 0.$$