

**Exercise 12**

Prove *Green's first identity*: For every pair of functions  $f(x)$ ,  $g(x)$  on  $(a, b)$ ,

$$\int_a^b f''(x)g(x) dx = - \int_a^b f'(x)g'(x) dx + f'g \Big|_a^b.$$