

Exercise 3

Prove the inequality $l \int_0^l (f'(x))^2 dx \geq [f(l) - f(0)]^2$ for any real function $f(x)$ whose derivative $f'(x)$ is continuous. [*Hint*: Use Schwarz's inequality with the pair $f'(x)$ and 1.]