

## Exercise 10

Prove the uniqueness of the Dirichlet problem  $\Delta u = f$  in  $D$ ,  $u = g$  on bdy  $D$  by the energy method. That is, after subtracting two solutions  $w = u - v$ , multiply the Laplace equation for  $w$  by  $w$  itself and use the divergence theorem.