

## Exercise 1

Prove that  $\Delta(\bar{u}) = \overline{(\Delta u)}$  for any function; that is, the laplacian of the average is the average of the laplacian. (*Hint:* Write  $\Delta u$  in spherical coordinates and show that the angular terms have zero average on spheres centered at the origin.)