

Exercise 10

Show that

$$\int_2^{e+1} \left(\frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^3} + \cdots \right) dx = 1, \quad x > 1$$