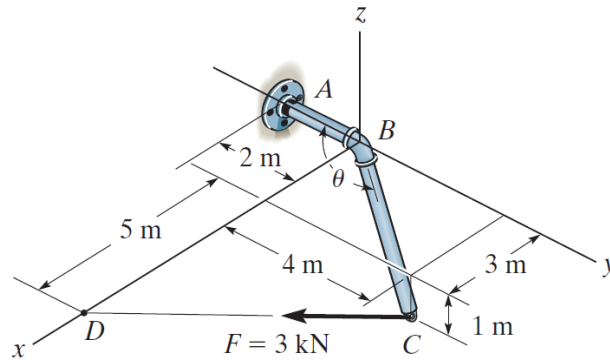


Problem 2-128

Determine the angle θ between BA and BC .



Probs. 2-128/129

Solution

Write the position vectors to the points A , B , and C .

$$\mathbf{r}_A = \langle 0, -2, 0 \rangle \text{ m}$$

$$\mathbf{r}_B = \langle 0, 0, 0 \rangle \text{ m}$$

$$\mathbf{r}_C = \langle 3, 4, -1 \rangle \text{ m}$$

The unit vector going from B to A is

$$\hat{\mathbf{u}}_{BA} = \frac{\mathbf{r}_A - \mathbf{r}_B}{|\mathbf{r}_A - \mathbf{r}_B|} = \frac{\langle 0, -2, 0 \rangle}{\sqrt{(0)^2 + (-2)^2 + (0)^2}},$$

and the unit vector going from B to C is

$$\hat{\mathbf{u}}_{BC} = \frac{\mathbf{r}_C - \mathbf{r}_B}{|\mathbf{r}_C - \mathbf{r}_B|} = \frac{\langle 3, 4, -1 \rangle}{\sqrt{(3)^2 + (4)^2 + (-1)^2}}.$$

Take the dot product of these unit vectors.

$$\cos \theta = \hat{\mathbf{u}}_{BA} \cdot \hat{\mathbf{u}}_{BC} = \frac{\langle 0, -2, 0 \rangle}{\sqrt{(0)^2 + (-2)^2 + (0)^2}} \cdot \frac{\langle 3, 4, -1 \rangle}{\sqrt{(3)^2 + (4)^2 + (-1)^2}} = -2\sqrt{\frac{2}{13}}$$

Therefore, the angle between the pipe segments is

$$\theta = \cos^{-1} \left(-2\sqrt{\frac{2}{13}} \right) \approx 142^\circ.$$