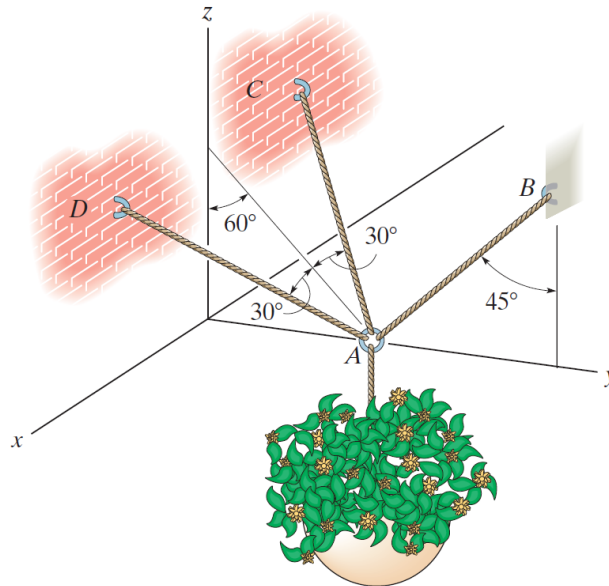


### Problem 3-57

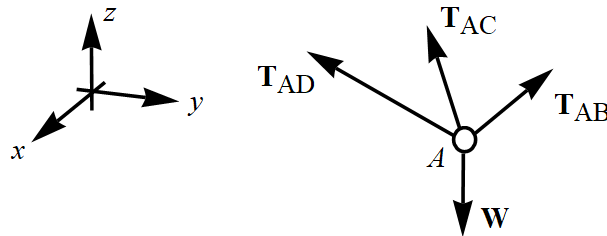
If each cord can sustain a maximum tension of 50 N before it fails, determine the greatest weight of the flowerpot the cords can support.



Probs. 3-56/57

#### Solution

Draw a free-body diagram for the ring at A.



In order for the system to be in equilibrium, the sum of the forces must be zero. Note that the angle that cord  $AB$  makes with the  $y$ -axis is  $45^\circ$ , and the missing angle of the triangle against the brick wall is  $30^\circ$ .

$$\mathbf{T}_{AB} + \mathbf{T}_{AC} + \mathbf{T}_{AD} + \mathbf{W} = \mathbf{0}$$

$$T_{AB}\hat{\mathbf{u}}_{AB} + T_{AC}\hat{\mathbf{u}}_{AC} + T_{AD}\hat{\mathbf{u}}_{AD} + W\langle 0, 0, -1 \rangle = \mathbf{0}$$

$$\begin{aligned} T_{AB}\langle 0, \cos 45^\circ, \sin 45^\circ \rangle + T_{AC}\langle -\sin 30^\circ, -\cos 30^\circ \cos 30^\circ, \cos 30^\circ \sin 30^\circ \rangle \\ + T_{AD}\langle \sin 30^\circ, -\cos 30^\circ \cos 30^\circ, \cos 30^\circ \sin 30^\circ \rangle + mg\langle 0, 0, -1 \rangle = \mathbf{0} \end{aligned}$$

Combine the vectors on the left side.

$$\begin{aligned} &\langle -T_{AC} \sin 30^\circ + T_{AD} \sin 30^\circ, \\ &\quad T_{AB} \cos 45^\circ - T_{AC} \cos 30^\circ \cos 30^\circ - T_{AD} \cos 30^\circ \cos 30^\circ, \\ &\quad T_{AB} \sin 45^\circ + T_{AC} \cos 30^\circ \sin 30^\circ + T_{AD} \cos 30^\circ \sin 30^\circ - mg \rangle = \langle 0, 0, 0 \rangle \end{aligned}$$

Match the components to get a system of equations.

$$\left. \begin{aligned} -T_{AC} \sin 30^\circ + T_{AD} \sin 30^\circ &= 0 \\ T_{AB} \cos 45^\circ - T_{AC} \cos 30^\circ \cos 30^\circ - T_{AD} \cos 30^\circ \cos 30^\circ &= 0 \\ T_{AB} \sin 45^\circ + T_{AC} \cos 30^\circ \sin 30^\circ + T_{AD} \cos 30^\circ \sin 30^\circ - mg &= 0 \end{aligned} \right\}$$

In the previous problem it was found that cord  $AB$  has the highest tension, so set  $T_{AB} = 50$  N and solve the system for  $T_{AC}$ ,  $T_{AD}$ , and  $mg$ .

$$T_{AC} = \frac{50\sqrt{2}}{3} \text{ N} \approx 23.6 \text{ N}$$

$$T_{AD} = \frac{50\sqrt{2}}{3} \text{ N} \approx 23.6 \text{ N}$$

$$mg = \frac{25}{3}(3\sqrt{2} + \sqrt{6}) \text{ N} \approx 55.8 \text{ N}$$