

**Exercise 14**

Solve the homogeneous wave equation on the half-line  $(0, \infty)$  with zero initial data and with the Neumann boundary condition  $u_x(0, t) = k(t)$ . Use any method you wish.